# Active schedules and a new hybrid genetic algorithm for the job shop scheduling problem

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**Abstract.** Active schedules and a new genetic algorithm for solving job shop scheduling problem are presented in this paper. In the proposed method, a chromosome representation of the problem is natural numbers, the GT algorithm is used to generate a set of active solutions, the mutation is implemented on the all machines concurrently. Especially, we propose a new crossover operator that combines the uniform crossover operator with GT algorithm and is implemented on 3 parents. The approach was tested on a set of benchmark programs and compared with other approaches. The computation results validated the effectiveness of the proposed algorithm.

Keywords: Jobshop, Scheduling, Schedule, Genetic Algorithm.

## 1. Introduction

Research in scheduling theory has evolved over the past fifty years and has been the subject of much significant literature with techniques ranging from unrefined dispatching rules to highly sophisticated parallel branch and bound algorithms and bottleneck based heuristics. Not surprisingly, approaches have been formulated from a diverse spectrum of researchers ranging from management scientists to production workers. However with the advent of new methodologies, such as neural networks and evolutionary computation, researchers from fields such as biology, genetics and neurophysiology have also become regular contributors to scheduling theory emphasising the multidisciplinary nature of this field.

The job shop scheduling problem - JSP is well known as one of the most difficult NP-hard ordering problems. In fact, we only know of few polynomially solvable cases of the JSP. Most JSP are NP-hard [1]. There have been some approaches for solving the JSP. For example, the *branch and bound* approach the *shifting bottle-neck* approach, the *simulated annealing* approach, *Genetic Algorithm-GA* methods etc. Recently, many researchers have used *hybrid* methods to solve JSP such as Chaoyong Zhang et al. [2], Lee Hui Peng et al. [3], M. Chandrasekaran [4], F. Guerriero [5], Rui Zhang et al. [6], etc. If JSP has been interested so much, it was because the importance of JSP both in theory and practice. This paper propose a new genetic algorithm for solving job shop scheduling problem.

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#### 2. Problem description

The JSP can be described as following:

A set of n jobs  $\{J_i\}_{1 \le j \le n}$  which is to be on a set of machines  $\{M_j\}_{1 \le j \le m}$ . The problem can be characterized as:

1. Each job must be processed on each machine in the order given in a pre-defined technological sequence of machines.

2. Each machine can process only one job at a time.

3. The operation of job  $J_i$  is processed on machine  $M_i$  is called the operation  $O_{ij}$ .

4. The processing time of  $O_{ij}$  is denoted  $p_{ij}$ .

5. The starting time and completion time of an operation  $O_{ij}$  is denoted as  $s_{ij}$  and  $c_{ij}$ .

6. The time required to complete all the jobs is called the *makespan*, which is denoted as  $C_{max}$ . By definition,  $C_{max} = \max \{c_{ij}\}_{1 \le i \le n, 1 \le j \le m}$ .

#### 3. Active schedules [5] and GT algorithm [7]

Schedules can be classified into one of following three types of schedules:

• Semi-active schedule: These feasible schedules are obtained by sequencing operations as early as possible. In a semi-active schedule, no operation can be started earlier without altering the processing sequences.

• Active schedule: These feasible schedules are schedules in which no operation could be started earlier without delaying some other operation or breaking a precedence constraint. Active schedules are also semi-active schedules. An optimal schedule is always active, so the search space can be safely limited to the set of all active schedules.

• Non-delay schedule: These feasible schedules are schedules in which no machine is kept idle when it could start processing some operation. Non-delay schedules are necessarily active and hence also necessarily semi-active.



Fig. 1. Types of Schedules.

The JSP is given by the job sequence matrix  $\{T_{ik}\}$  and processing time matrix  $\{p_{ik}\}$ . An active schedule can be generated by using the GT algorithm proposed by Giffler & Thompson [7]. The algorithm is described as following:

1. Initialize *G* as a set of operations that are first in the technological sequence (the first column of the matrix  $\{T_{ik}\}$ , i.e.  $G = \{O_{1T_{11}}, O_{2T_{21}}, ..., O_{nT_{n1}}\}$ . For each operation  $O \in G$ , ES(O) := 0 and EC(O) := p(O).

2. Find the earliest complete operation  $O_{*i} \in G$ . A subset of *G* that consists of operations processed on machine  $M_i$  is denoted  $G_i$  (by 2.1).

3. Calculate the conflict set  $C[M_j, k] \subset G_j$  where k -1 is the number operations already scheduled on  $M_j$  (by 2.2).

4. Select one of the operations in  $C[M_{i}, k]$  randomly. Let the selected operation be  $O_{i*i}$ .

5. Schedule  $O_{i*j}$  as  $k^{th}$  operation on  $M_j$ ; i.e.  $S_{jk} := i^*$ , with its starting and completion times equal to  $ES(O_{i*j}) \& EC(O_{i*j}) : S(O_{i*j}) = ES(O_{i*j}); c(O_{i*j}) = EC(O_{i*j}).$ 

6. For all operations  $O_{ij} \in G_j \setminus \{O_{i*j}\}$ :

- Update  $ES(O_{ij})$  as:  $ES(O_{ij}) := \max\{ES(O_{ij}), EC(O_{i*j})\}$ .

- Update  $EC(O_{ij})$  as:  $EC(O_{ij}) := ES(O_{ij}) + p(O_{ij})$ .

7. Remove  $O_{i*j}$  from G, and add an operation  $O_{is}$  that is the next to  $O_{i*j}$  in the technological sequence of  $J_i$  to G if such  $O_{is}$  exits. i.e., if  $j = T_{ik}$  and k < m, then  $s := T_{ik+1}$  and  $G := (G \setminus \{O_{i*j}\} \cup \{O_{is}\})$ . Calculate  $ES(O_{is})$  and  $EC(O_{is})$  as:

 $- ES(O_{is}) := \max\{EC(O_{i*j}), EC(PM(O_{is}))\}.$ 

 $- EC(O_{is}) := ES(O_{is}) + p(O_{is}).$ 

8. Repeat from step 1 to step 7 until all operations are scheduled.

9. Output the solution matrix  $\{S_{jk}\}$  as the active schedule obtained with set of starting and completion times  $\{s(O_{ij})\}\$  and  $\{c(O_{ij})\}\$ , where  $i = S_{jk}$ .

#### 4. The proposed genetic algorithm

#### 4.1 Solution coding

We suppose there are n jobs are given to be processed on m machines. The number of operations of job  $J_i$  is denoted job[i] ( $job[i] \le m$ , with every *i*). The sum of operations has to process of the all

jobs are  $L = \sum_{i=1}^{n} j_{ob}[i]$ . We code operations of  $J_1$  from 1 to  $j_{ob}[1]$ , of  $J_2$  from  $j_{ob}[1] + 1$  to  $j_{ob}[1] + 1$ 

job[2],..., of  $J_n$  from job[1] + job[2] + ... + job[n-1] + 1 to L. Thus, one solution is one certain permutation of the natural numeral chain  $\{1, 2, 3, ..., L\}$  satisfy of the problem constraints.

By definition,  $C_{max} = \max\{c_{ij}\}_{1 \le i \le n, 1 \le j \le m}$ .

Job	Machine (processing time)								
1	1 (3)	2 (3)	3 (3)						
2	1 (2)	3 (3)	2 (4)						
3	2 (3)	1 (2)	3 (1)						

Table 1. The JSP with 3 jobs and 3 machines

The problem is equivalently represented by the job sequence matrix  $\{T_{ik}\}$  and processing time matrix  $\{p_{ik}\}$  as following:

	1	2	3		3	3	3
$\left\{T_{ik}\right\} =$	1	3	2	$\{p_{ik}\}=$	2	3	4
	2	1	3		3	2	1

For example, the problem with 3 jobs and 3 machines given in Table 1. Operations are coded by natural numbers as in Table 2.

	Jobs		Operation coding					
	$J_1$	1			2		3	
	$J_2$	4			5		6	
	$J_3$		7		8	8		)
1	2	3	4	5	6	7	8	9
1	4	8	7	6	2	5	3	9
$J_1$	$J_2$	<b>J</b> <sub>3</sub>	$\int J_3$	$J_2$	$J_1$	$, \underbrace{J_2}$	$J_1$	J <sub>3</sub>
	$M_1$			M			M	,

Table 2. The operations are coded by natural numbers

Fig. 2. A valid solution for the problem job shop  $3 \times 3$ .

Explanation: According to  $\{T_{jk}\}$ , operations 1, 4, 8 are processed on machine 1. Thus, codes on the  $M_1$  are one certain permutation of the chain  $\{1, 4, 8\}$ . Similarly, codes on the  $M_2$  are one certain permutation of the chain  $\{2, 6, 7\}$ , codes on the  $M_3$  are one certain permutation of the chain  $\{3, 5, 9\}$ . A valid solution for the problem may be as Figure 2. This solution can be showed by a solution matrix  $S_{jk}$ . Where,  $S_{jk} = i$ , means that  $k^{th}$  operation on machine  $M_j$  is job  $J_i$ .

$$\{S_{jk}\} = \begin{vmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \\ 2 & 1 & 3 \end{vmatrix}$$

#### 4. 2 Generating a set initial solutions

JSP represented by the technological sequence matrix  $\{T_{ik}\}$ , and the processing time matrix  $\{p_{ik}\}$ . A initial active schedule for the problem can be generated by using the GT algorithm [6] presented in the section 3.

#### 4.3 Construct fitting function

The fitting function is represented as following:

 $Fitness = M - C_{max}$ , there  $C_{max}$  is makespan of the solution, M is parameter given for change min problem to max problem (because genetic algorithm only applies immediately for max problem).

#### 4.4 Genetic operators

#### a) Selection operator

According to Darwin's evolution theory the best ones should survive and create new offspring. There are many methods to select the best chromosomes. In this paper, we use the "Roulette Wheel Selection". Parents are selected according to their fitness. The better the chromosomes are, the more chances to be selected they have.

b) Mutation operator

• Random selection of one operation (*ope1*) of parent. Define the machine ( $M_{ope1}$ ) which performs the operation that has just been selected and define the position (*pos1*) of this operation in the parent.

• Random selection one operation (*ope2*) of parent. Define the machine ( $M_{ope2}$ ) which performs the operation has just been selected and define the position (*pos2*) of this operation.

• If  $M_{ope1} = M_{ope2}$  then implement mutation. The getting result is child chromosome. On the other hand, the parent chromosome is kept intact.

• For all operations of the child chromosome, update its starting and completion times.

Example, the parent is selected for mutation as following:



Fig. 3. The parent chromosome for insert mutation.

- + For example:  $ope1 = 2 - > M_{ope1} = 2$  and pos1 = 6.
- $+ ope2 = 7 ---> M_{ope2} = 2 \text{ and } pos2 = 4.$

 $+ M_{ope1} = M_{ope2} - -->$  insert operation 2 in to position 4. We have child:

1	2	3	4	5	6	7	8	9
1	4	8	2	7	6	5	3	9
$J_1$	$J_2$	$J_3$	$J_1$	<u> </u>	$J_2$	, <b>J</b> 2	$J_1$	$J_3$
	Ň	<b>1</b> 1		۴N	<b>1</b> ,		'N	<b>1</b> 3

Fig. 4. The child chromosome after insert mutation.

The mutation operator is implemented on the all machines, then the random selection is implemented m times.

c) Crossover operator

$$p_{1} = \begin{vmatrix} 2 & 3 & 1 \\ 3 & 2 & 1 \\ 2 & 3 & 1 \end{vmatrix} \xrightarrow{22 \ 33111} 333 \ 2222111 \\ 333 \ 2222 \ 1111} \rightarrow \text{makespan} = 15$$

$$H_{ji} = \begin{vmatrix} 3 & 3 & 3 \\ 2 & 3 & 2 \\ 1 & 1 & 1 \end{vmatrix} \xrightarrow{1112233} p_{2} = \begin{vmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 3 & 1 & 2 \\ 3 & 1 & 2 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

$$p_{2} = \begin{vmatrix} 1 & 3 & 2 \\ 3 & 1 & 2 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

$$p_{3} = \begin{vmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

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$$p_{3} = \begin{vmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

$$p_{3} = \begin{vmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

Fig. 5. The uniform crossover use GT algoriths with 3 parents.

A scheduling problem represented by  $\{T_{ik}\}$ , the technological sequence matrix, and  $\{p_{ik}\}$ , the processing time matrix. The crossover operator combines the uniform crossover with GT algorithm and is implemented on 3 parents  $p_1$ ,  $p_2$  and  $p_3$ . This parents are showed by correlative solution matrixs  $S^1 = \{S^1_{jk}\}, S^2 = \{S^2_{jk}\}$  and  $S^3 = \{S^3_{jk}\}$ . Genes of offspring  $p = \{S_{jk}\}$  are ones from each parent. The crossover operator can be described as:



Fig. 6. The parents for crossover and the child chromosome after crossover.

1. Initialize G as a set of operations that are first in the technological sequence, i.e.,  $G = \{ O_{1T_{11}}, O_{2T_{21}}, ..., O_{nT_{n1}} \}$ . For each operation  $O \notin$ , ES(O) := 0 and EC(O) := p(O).

2. Find the earliest completable operation  $O_{*_j} \in G$ . A subset of *G* that consists of operations processed on machine  $M_j$  is denoted as  $G_j$ .

3. Calculate the conflict set  $C[M_j, k] \subset G_j$ , where k - 1 is the number of operations already scheduled on  $M_j$ .

4. Select on of the parents  $\{p_1, p_2, p_3\}$  as p according to the value of  $H_{ji}$ ,  $p := p_{H_{ij}}$  and  $S^p = s^{H_{ij}}$ . For earch  $O_{ij} \in C[M_j, k]$  with job number i, there exists an index 1 such that  $S_{jl} = i$ . Let  $l_m$  be the smallest index number among them, i.e.,  $l_m = \min \{l / S_{jl} = i \text{ and } O_{ij} \in C[M_j, k]\}$  and let  $r := S_{jlm}$ . This results in selecting an operation  $O_{rj} \in C[M_j, k]$  that has been scheduled in p earliest among the members of  $C[M_j, k]$ .

5. Schedule  $O_{rj}$  as the  $k^{th}$  operation on  $M_j$ ; i.e.  $S_{jk} := r$ , with its starting and completion times equal to  $ES(O_{rj})$  and  $EC(O_{rj})$  respectively:  $s(O_{rj}) = ES(O_{rj})$ ;  $c(O_{rj}) = EC(O_{rj})$ .

6. For all  $O_{ij} \in G_i \setminus \{O_{ri}\}$  update:

-  $ES(O_{ij})$  as:  $ES(O_{ij}) := \max\{ES(O_{ij}), EC(O_{rj})\}.$ 

-  $EC(O_{ii})$  as:  $EC(O_{ii}) := ES(O_{ii}) + p(O_{ii})$ .

7. Remove  $O_{rj}$  from G (and therefore from  $G_j$ ), and add operation  $O_{rs}$  that is the next to  $O_{rj}$  in the technological sequence to G if such  $O_{rs}$  exists; i.e., if  $j = T_{ik}$  and k < m, then  $s := T_{i,k+1}$  and G := $(G \setminus \{O_{ri}\} \cup \{O_{rs}\})$ .

Calculate  $ES(O_{rs})$  and  $EC(O_{rs})$  as:

 $- ES(O_{rs}) := \max\{EC(O_{rj}), EC(PM(O_{rs}))\}.$ 

 $- EC(O_{rs}) := ES(O_{rs}) + p(O_{rs}).$ 

8. Repeat from step 1 to step 7 until all operations are scheduled.

9. Output the solution matrix  $\{S_{ik}\}$  as the active schedule obtained with the set of starting and completion times  $\{s(O_{ij})\}\$  and  $\{c(O_{ij})\}\$  respectively, where  $i = S_{jk}$ . Figure 8 shows an example of the uniform crossover operator with GT algorithm and is implemented on 3 parents  $p_1$ ,  $p_2$  and  $p_3$  with an inheritance matrix  $H_{ii}$ .

The parents for crossover and the child chromosome after crossover are showed by picture as Figure 6.

#### 4.5 Evolutional algorithm

The evolutional algorithm for the job shop problem is described as following:

Procedure GA\_JSP Begin t = 0Initialize P(t){using GT algorithm} Evaluate P(t)While not termination condition do Begin Build intermediate solution set P'(t): - Perform the mutation operator for P(t), we get  $P_1(t)$ - Perform the crossover operator for P(t), we get  $P_2(t)$  $-P'(t) = P(t) \cup P_1(t) \cup P_2(t)$ Evaluate P'(t)t = t + 1Select P(t) from P'(t-1)Evaluate P(t)If  $\text{Eval}(P(t - 1)) \ge \text{Eval}(P(t))$  then t = t - 1End End

#### 5. Experimental results

Based on the proposed method, we implemented a program to find an optimal schedule for the JSP. The program ran on the PC with Core 2 Dual CPU and is applied to Muth and Thompson's benchmark problems. The results as in Table 3. Among the research works applied GA to the JSP,

Methods proposed by Yamada are counted as one of the best methods until now. Thus, for the sake of comparison we is chosen the GA and GT/GA methods of Yamada [8] in Table 4 and Table 5.

Problems	Population Size	Generation number	Crossover rate (pc)	Mutation rate (p <sub>m</sub> )	result	Real optimal result
mt06 ( $6 \times 6$ )	50	200	0.5	0.05	55	55
mt10 ( $10 \times 10$ )	500	200	0.8	0.05	930	930
mt20 ( $20 \times 5$ )	500	200	0.8	0.05	1185	1165

Table 3. Experimental results of the proposed method

Table 4. Experimental results of the SGA method of Yamada

Problems	Population	Generation	Crossover	Mutation	1.	Real optimal
	sıze	number	rate (pc)	rate (pm)	result	result
mt06	100	200	0.9	0.01	55	55
mt10	1000	200	0.9	0.01	965	930
mt20	2000	200	0.9	0.01	1215	1165

Table 5. Experimental results of the GA/GT method of Yamada

Problems	Population size	Generation number	Crossover rate (pc)	Mutation rate (pm)	result	Real optimal result
mt066	100	200	0.9	0.01	55	55
mt10	1000	200	0.9	0.01	930	930
mt20	2000	200	0.9	0.01	1184	1165

## 6. Conclusion

In this paper we presented of active schedules and proposed a new genetic algorithm for the JSP. In the proposed method, we sensibly combined of the results of the predecessors with our new propositions. We proposed a genetic algorithm for the JSP with a new crossover operator. Base on proposed method, we implemented a program to find an optimal schedule for the JSP. The program ran with inputs are the mt benchmark problems and provided good results. The program gave the real optimal solution with small and medium-sized testing problems. However, for the large-sized testing problems as mt20, the proposed method has not found an optimal solution. In the future, we will try to find new genetic operators more suitable for the JSP.

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