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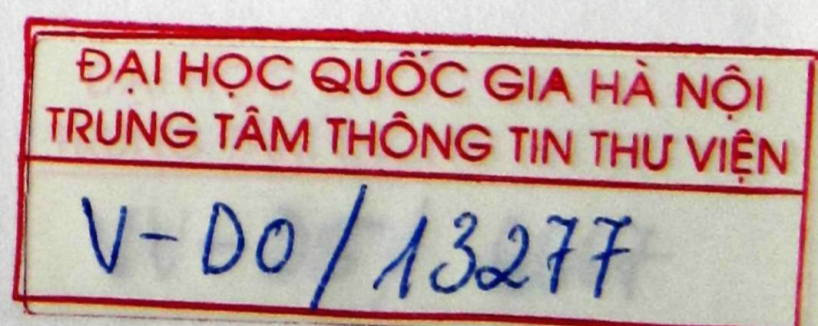
# NHỮNG PHƯƠNG PHÁP TIỆM CẬN CỦA ĐỘNG LỰC HỌC PHI TUYẾN

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**NHÀ XUẤT BẢN ĐẠI HỌC QUỐC GIA HÀ NỘI**

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