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Applied Asymptotic Methods in Nonlinear Oscillations

by

YU. A. MITROPOLSKII

*Institute of Mathematics,
Kiev, Ukraine*

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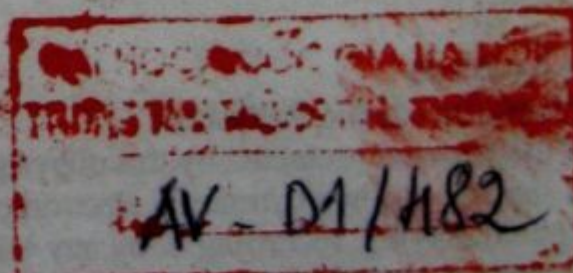
NGUYEN VAN DAO

*Vietnam National University,
Hanoi, Vietnam*



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