

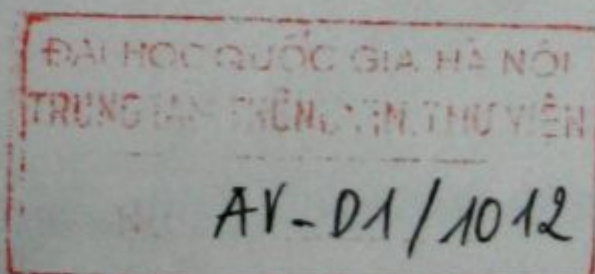
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LINEAR ALGEBRA AND ITS APPLICATIONS

THIRD EDITION

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CONTENTS

Preface

ix

1 MATRICES AND GAUSSIAN ELIMINATION

1.1	Introduction	1
1.2	The Geometry of Linear Equations	3
1.3	An Example of Gaussian Elimination	12
1.4	Matrix Notation and Matrix Multiplication	19
1.5	Triangular Factors and Row Exchanges	31
1.6	Inverses and Transposes	42
1.7	Special Matrices and Applications	52
	Review Exercises	60

2 VECTOR SPACES AND LINEAR EQUATIONS

2.1	Vector Spaces and Subspaces	63
2.2	The Solution of m Equations in n Unknowns	71
2.3	Linear Independence, Basis, and Dimension	80
2.4	The Four Fundamental Subspaces	90
2.5	Networks and Incidence Matrices	102
2.6	Linear Transformations	116
	Review Exercises	128

3 ORTHOGONALITY

3.1	Perpendicular Vectors and Orthogonal Subspaces	132
3.2	Inner Products and Projections Onto Lines	144
3.3	Projections and Least Squares Approximations	153
3.4	Orthogonal Bases, Orthogonal Matrices, and Gram-Schmidt Orthogonalization	166
3.5	The Fast Fourier Transform	183
3.6	Review and Preview	195
	Review Exercises	208

4 DETERMINANTS

4.1	Introduction	211
4.2	The Properties of the Determinant	214
4.3	Formulas for the Determinant	222
4.4	Applications of Determinants	231
	Review Exercises	241

5 EIGENVALUES AND EIGENVECTORS

5.1	Introduction	243
5.2	The Diagonal Form of a Matrix	254
5.3	Difference Equations and the Powers A^k	262
5.4	Differential Equations and the Exponential e^{At}	275
5.5	Complex Matrices: Symmetric vs. Hermitian and Orthogonal vs. Unitary	290
5.6	Similarity Transformations	304
	Review Exercises	319

6 POSITIVE DEFINITE MATRICES

6.1	Minima, Maxima, and Saddle Points	322
6.2	Tests for Positive Definiteness	330
6.3	Semidefinite and Indefinite Matrices; $Ax = \lambda Mx$	339
6.4	Minimum Principles and the Rayleigh Quotient	347
6.5	The Finite Element Method	355

7 COMPUTATIONS WITH MATRICES

7.1	Introduction	361
7.2	The Norm and Condition Number of a Matrix	363
7.3	The Computation of Eigenvalues	370
7.4	Iterative Methods for $Ax = b$	380

8 LINEAR PROGRAMMING AND GAME THEORY

8.1	Linear Inequalities	388
8.2	The Simplex Method and Karmarkar's Method	395
8.3	The Theory of Duality	412
8.4	Network Models	424
8.5	Game Theory and the Minimax Theorem	433
PREFACE		
APPENDIX A	THE SINGULAR VALUE DECOMPOSITION AND THE PSEUDOINVERSE	442
APPENDIX B	THE JORDAN FORM	453
APPENDIX C	COMPUTER CODES FOR LINEAR ALGEBRA	461
<i>References</i>		472
<i>Solutions to Selected Exercises</i>		473
<i>Index</i>		499