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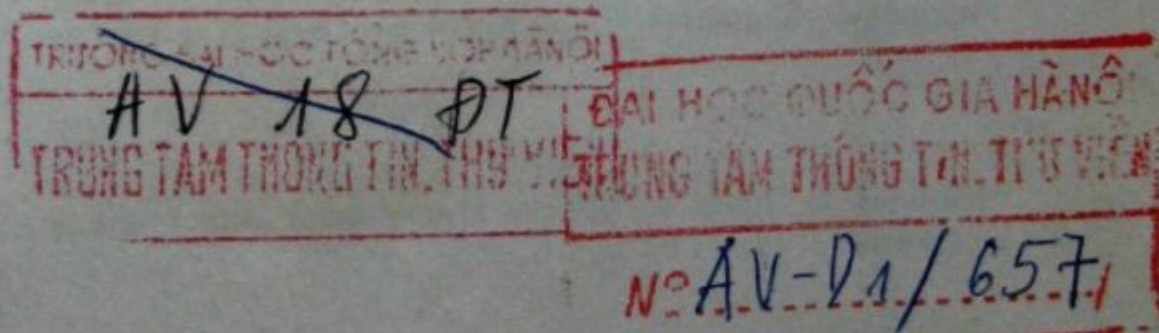
Foundations of Optimization

second edition

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Prentice Hall of India Private Limited

New Delhi-110001

1982

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