

A variation-of-constants formula for abstract functional differential equations in the phase space

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Abstract: For linear functional differential equations with infinite delay in a Banach space, a variation-of-constants formula is established in the phase space. As an application one applies it to study the admissibility of some spaces of functions whose spectra are contained in a closed subset of the real line. ?? 2002 Elsevier Science.

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